Names

With your partner(s), read through the instructions and do the activities described. Discuss your questions, ideas, and findings with each other. Write your results and/or answers on this worksheet. You may attach graphs and/or printouts if they are explained and are useful to your report. Only one report should be submitted from each group. This report is due Monday.

1. Introduction to WolframAlpha.

Start-up: Open an internet browser and navigate to http://www.wolframalpha.com/.

Fun stuff and graphs: Enter each of the following phrases. Look at the kind of information included in the response. For each graph that is displayed, <u>record</u> here the dependent and independent variables.

- Height and weight
- Goshen College
- Goshen Indiana weather
- IBM
- Carbon
- A group member's name

Simple calculations: Enter each of the following calculations and <u>record</u> the answers. Make sure you understand why these answers are given.

- 3*4 + 1
- 5 + 3 * 2
- 10/8
- 5^2
- 18^-(1/2)
- cos(3)
- (a+b)^2

2. Graphs. Enter each of the following.

- graph $(x^2-x)/(x^2+1)$
- graph $(x^2-x)/(x^2+1)$ with x from -1 to 2
- graph $(x^2-x)/(x^2+1)$ with x from -100 to 100
- graph $(x^2-x)/(x^2+1)$ with x from -15 to 15 and y from -0.3 to 1.3

Describe the features of the graph of

$$y = (x^2 - x) / (x^2 + 1)$$

that are revealed by the last graph. <u>State</u> the features that are not revealed by the second and third graphs. Describe the output for the first graph, which did not explicitly give a viewing window.

A graph of an equation is a *complete graph* if it suggests all points of the graph and all of the important features of the graph. Use WolframAlpha to obtain a complete graph of

$$y = x^3 + 408x^2 - 123x + 59$$

Sketch by hand the graph you obtained. Estimate the solution(s) of

 $x^3 + 408x^2 - 123x + 59 = 0$

from your graph.

3. Solving Equations Graphically. An equation of the form

$$f(x) = c$$

can be solved by identifying where the graph of

$$y = f(x)$$

crosses the horizontal line

$$y = c$$

WolframAlpha accepts the word *solve* to find solutions and provide a graph. For each of the following equations, find all real-value solutions to at least four significant digits. <u>Sketch by</u> <u>hand</u> a graph that displays all solutions. <u>Label</u> the scales on the axes and the solutions.

a.
$$x^3 - 65x + 10 = 0$$

b.
$$x^4 - 3x^3 - 6x + 5 = 0$$

c.
$$x^3 - 2x^2 + 3x = 5$$

d.
$$x^3 - 3x^2 = -4$$

e.
$$x^3 - 4x^2 + x + \frac{172}{25} = 0$$

f.
$$x^3 + 408x^2 - 123x + 59 = 0$$

4. **Reading graphs.** Obtain a complete graph of $|x^2 - 4|$

Look at your graph and consider the equation

$$\left|x^2 - 4\right| = c$$

<u>Record</u> the following.

- a. Find a value of c for which this equation has four solutions.
- b. Find a value of c for which this equation has three solutions.
- c. Find a value of c for which this equation has two solutions.
- d. Find a value of c for which this equation has no solutions.
- e. Is there any other possible number of solutions of this equation? Explain.

5. **Simplification.** For each of the following expressions, command WolframAlpha to simplify, expand, and factor. <u>Record</u> the responses and explain why each response is reasonable.

 $x^4 - 4x^3 - x^2 + 4x$

$$(x^{2} + x - 3)(x^{2} + x + 1)$$

$$\frac{2}{x^2 - 1} - \frac{5}{x^2 - 3x - 4}$$