

1. Let  $u = (3, 4)$  and  $v = (-5, 12)$ . Compute

(a) the lengths of  $u$  and  $v$ .

(b) the unit vectors of  $u$  and  $v$ .

(c) the dot product of  $u$  and  $v$ .

Use your computations to determine whether the angle between  $u$  and  $v$  is acute, right, or obtuse. Draw  $u$  and  $v$  to check.

2. Let  $u = 2\hat{i} - 3\hat{j}$  and  $v = 3\hat{i} + \hat{j}$ . The goal of this exercise is to write  $u$  as the sum of two vectors  $u_1$  and  $u_2$  where  $u_1$  is parallel to  $v$  and  $u_2$  is perpendicular to  $v$ . The vector  $u_1$  is called the *projection of  $u$  onto  $v$* .

(a) How long is the projection of  $u$  onto  $v$ ? Draw a triangle and use trigonometry.

(b) Since a vector is determined by its length and direction, we next determine the direction of the projection. What should the unit vector for the projection be?

(c) Combine your answers to the previous two questions to determine  $u_1$ .

(d) Now that you have  $u$  and  $u_1$ , find  $u_2$ .

(e) Draw all four vectors on the same set of coordinate axes.