

**Derivatives of Simple Functions.**

- **Constant Functions:**  $c$  (not depending on  $x$ ). Examples  $f(x) = 5$ ,  $g(x) = e$ ,  $h(x) = \ln(2)$ .

$$\frac{d}{dx} c =$$

- **Power Functions:**  $x^a$ . Examples:  $x^3$ ,  $x^{2/3} = \sqrt[3]{x^2}$ ,  $x^{-4} = 1/x^4$ .

$$\frac{d}{dx} x^a =$$

- **Exponential Functions:**  $a^x$  ( $a > 0$ ,  $a \neq 1$ ). Examples:  $2^x$ ,  $(1/3)^x$ ,  $e^x$ .

$$\frac{d}{dx} e^x =$$

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- **Logarithmic Functions:**  $\log_a x$  ( $a > 0$ ,  $a \neq 1$ ). Examples:  $\log_2 x$ ,  $\log x$ ,  $\ln x$ .

$$\frac{d}{dx} \ln x =$$

$$\frac{d}{dx} \log_a x =$$

**Differentiation Rules.** Suppose  $a$  and  $b$  are constants and  $f$  and  $g$  are differentiable functions.

- **Constant Multiple Rule, Sum and Difference Rules:**

$$\frac{d}{dx} (af(x) \pm bg(x)) =$$

- **Product and Quotient Rules:**

$$\frac{d}{dx} f(x) \cdot g(x) =$$

$$\frac{d}{dx} \frac{f(x)}{g(x)} =$$

- **Chain Rule:**

$$\frac{d}{dx} f(g(x)) =$$

**Simple Antiderivatives.**

- **Constant Functions:**  $c$  (not depending on  $x$ ),

$$\int c \, dx =$$

- **Some Power Functions:**  $x^a$  ( $a \neq -1$ ),

$$\int x^a \, dx =$$

- **Exponential Functions:**  $a^x$  ( $a > 0, a \neq 1$ ),

$$\int e^x \, dx =$$

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- **The Reciprocal Function:**  $1/x = x^{-1}$

$$\int \frac{1}{x} \, dx =$$

**Substitution:**  $\int f(u(x)) u'(x) \, dx = \int f(u) \, du$

- $\int (3x + 4)^8 3 \, dx =$

- $\int (4x + 1)^9 \, dx =$

- $\int (1 - x)^6 \, dx =$

- $\int 2x e^{x^2} \, dx =$

- $\int \frac{1}{2x - 1} \, dx =$