

Name: _____

Section: _____

You have 30 minutes to complete the following problems, without using your notes, book, or calculator.

Part 1: Algebraic and Exponential Functions

1. Classify each function given below, by circling the appropriate name or names.

(a) $f(x) = 2^x$

root power polynomial exponential

(b) $g(x) = x^5$

rational power root polynomial

(c) $h(x) = \frac{x}{2x-1}$

algebraic power rational root

(d) $Q(t) = t^{1/4}$

power root exponential rational

(e) $P(x) = x^3 - 6x + 4$

linear power algebraic polynomial

2. State the domain of each function from the previous problem.

(a) _____

(b) _____

(c) _____

(d) _____

(e) _____

3. Find a formula for a linear function $f(x)$ whose graph passes through $(3, 1)$ and has a slope of 2.
4. Find a formula for an exponential function $Q(t)$ whose initial value is $Q(0) = 27$ and which decreases by one third for every unit time: $Q(1) = 9$, $Q(2) = 3$, etc.

Part 2: Trigonometry

5. Fill in the following table, using the five standard angles in the first quadrant.

Angle, θ		$\sin \theta$	$\cos \theta$	$\tan \theta$
deg	rad			

6. Evaluate the function at the given value.

(a) $\cos(-150^\circ) =$ _____

(b) $\sec(\frac{5\pi}{3}) =$ _____

Part 3: Logarithms

7. Find the exact value of the given quantity:

(a) $\ln(1) =$ _____

(b) $\ln(e^3) =$ _____

(c) $e^{-3 \ln 2} =$ _____

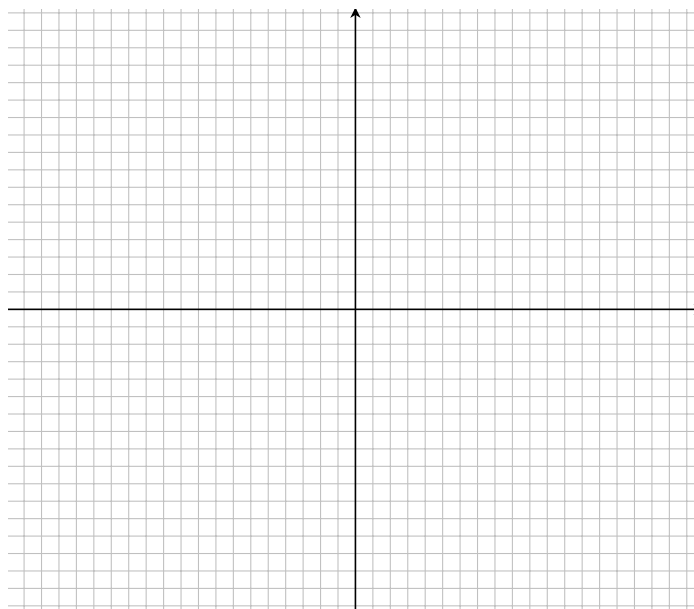
8. Express $\ln 4 - \ln 5 + 3 \ln 3$ as a single logarithm: _____. (Show your work below.)

9. Consider the function $f(x) = \ln(x + 2)$. Give the domain, range, and x -intercept in the spaces provided, and sketch the graph on the axes provided. Make sure to provide scale on each axis.

Domain: _____

Range: _____

x -intercept: _____



Part 4: Inverse Functions and Inverse Trig Functions

10. Determine whether each function is one-to-one. If it is one-to-one, sketch a graph of its inverse on the same set of axes.

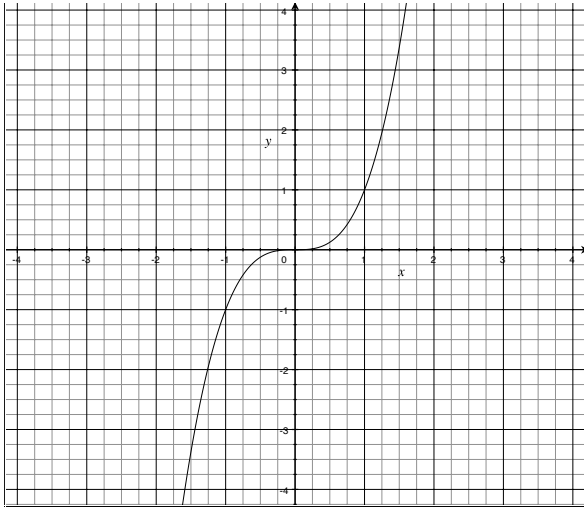


Figure 1: Is this function one-to-one? Y/N

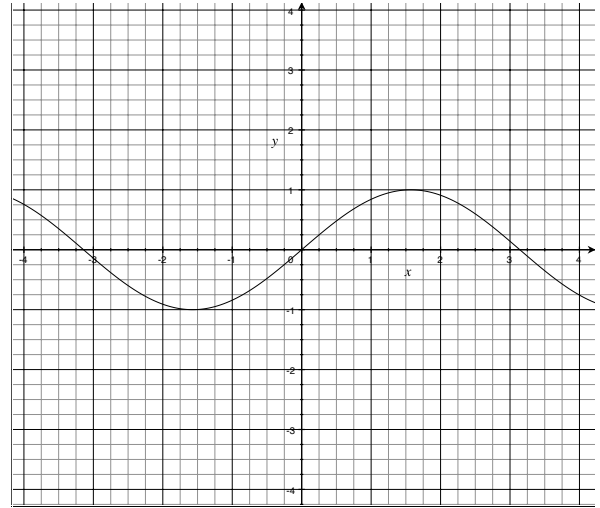


Figure 2: Is this function one-to-one? Y/N

11. Find the exact value of the given quantity:

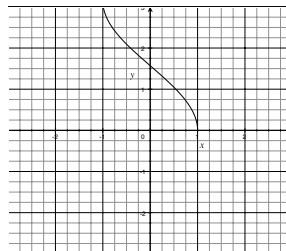
(a) $\cos^{-1}\left(\frac{\sqrt{3}}{2}\right) = \underline{\hspace{2cm}}$

(b) $\tan^{-1}(1) = \underline{\hspace{2cm}}$

(c) $\arcsin(0) = \underline{\hspace{2cm}}$

12. The graph of which function is depicted below?

$$f(x) = \arcsin(x) \qquad g(x) = \cos^{-1}(x) \qquad h(x) = \sec(x) \qquad r(x) = \arctan(x)$$



Part 5: Composition of Functions

13. Find formulas for the functions
- $f \circ g$
- and
- $g \circ f$
- , where

$$f(x) = 2x + 3 \quad \text{and} \quad g(x) = \sin x$$

$$(f \circ g)(x) = \underline{\hspace{2cm}}$$

$$(g \circ f)(x) = \underline{\hspace{2cm}}$$

14. Express the function in the form
- $f \circ g$
- .

(a) $F(x) = (x - 2)^2$

$$f(x) = \underline{\hspace{2cm}}$$

$$g(x) = \underline{\hspace{2cm}}$$

(b) $G(x) = \tan^2(x)$

$$f(x) = \underline{\hspace{2cm}}$$

$$g(x) = \underline{\hspace{2cm}}$$

(c) $H(x) = \frac{2x}{2x - 3}$

$$f(x) = \underline{\hspace{2cm}}$$

$$g(x) = \underline{\hspace{2cm}}$$