## This exam covers:

- Techniques of Integration: substitution, ibp, partial fractions, trig substitution (7.1, 7.2, 7.4)
- Limits and Improper Integrals: the limit of the values of a function, infinite limits, limits at infinity, indeterminate forms, L'Hopital's rule, convergent and divergent integrals (1.7, 1.8, 1.9, 4.7, 7.6)
- Parametric Equations: parametric equations of motion, velocities in x and y directions, speed, parametric curves: slope, concavity, area (4.8 and supplementary notes)

Textbook exercises for review, priority in bold:

- Ch 1 Review: 44, 45, 46
- Ch 4 Review: 7\*, 8\*, 9\*, 37, 38, 82, 83, 84, 85 \*Find the limits only.
- Ch 7 Review: 3-69, **72**, 77-78, **88**, 112, 115, 119, **120**, 122, 125, 126a, 128-134, **132**, 140-151, **143**, 154, **181**, **189**

Additional exercises for review, priority in bold:

- 1. Consider the parametric equations  $x = \sqrt{t}$ , y = 1/t.
  - (a) Find an equation for the tangent line to the curve at the point (1,1).
  - (b) Determine whether the curve is concave up or concave down at the point (1,1).
  - (c) Find the area under the curve from x = 1 to x = 4.
- 2. Consider the parametric equations  $x = 2t^3 + 1$ ,  $y = t^2$ .
  - (a) Find the area encosed by the curve and the x-axis from x = 1 to x = 3 by setting up and evaluating an integral in terms of t.
  - (b) Check your answer by eliminating the parameter to obtain a Cartesian equation for the curve and integrating with respect to x.
- 3. Consider the parametric equations x = 2t,  $y = 3 3t^2$ 
  - (a) Find the area between the curve and the x-axis by setting up and evaluating an integral in terms of t.
  - (b) Check your answer by eliminating the parameter to obtain a Cartesian equation for the curve and integrating with respect to x.
- **4**. The motion of a reflector on a bicycle wheel of radius 1 is given by  $x = t \sin t$ ,  $y = 1 \cos t$ . The path traced out by the reflector is a curve called a **cycloid**.
  - (a) Find the velocity of the reflector in the x-direction, the velocity of the reflector in the y-direction, and the speed of the reflector at arbitrary time t.
  - (b) Are there any moments when the reflector is momentarily paused? When its motion is purely up and down? Purely left and right?
  - (c) Find the horizontal and vertical tangents of the cycloid.
  - (d) Where is the cycloid concave up? Concave down?
  - (e) Sketch the cycloid by plotting x and y coordinates for  $t = 0, \frac{\pi}{2}, \pi, \frac{3\pi}{2}, 2\pi, \dots$
  - (f) Find the area under one arch of the cycloid.