

Writing assignment:

Suppose you are a hiker standing on the graph of the function $f(x, y) = 2e^{-(x^2+y^2)}$, directly above the point $(\frac{1}{2}, -\frac{1}{2})$ in the xy -plane. Explain what partial derivatives, the gradient, directional derivatives, and the differential tell you about the terrain in your immediate vicinity.

Guide for your work:

A fully complete writing assignment will include the steps outlined below as well as additional discussion of the key ideas and how they are connected.

- (a) Suppose due north is in the \hat{j} direction in the xy -plane. What is the slope of your path if you hike due north? Due south? Due east? Due west?
- (b) What is the slope of your path if you hike 30° east of north? What is the slope of your path if you hike in the direction of steepest ascent? What compass direction is the direction of steepest ascent?
- (c) Find the differential df at $(\frac{1}{2}, -\frac{1}{2})$, and explain how it can be used to estimate your change in elevation if you hike only a short distance from your initial point.
- (d) Sketch a contour diagram for the graph of $f(x, y)$, and use it to check that your answers above make sense.