

Name: \_\_\_\_\_

Read the first part of Section 4.1, up to and including the proof of Theorem 4.9.

**Reading Questions**

1. Make sure you know the definitions of cyclic group, generator of a cyclic group, and the order of an element in a group.
2. Reread Example 4.5. Consider the group  $\mathbb{Z}_4$ . Is  $\mathbb{Z}_4$  a cyclic group? If so, what elements of  $\mathbb{Z}_4$  are generators? Find the order of each element in  $\mathbb{Z}_4$ .

(Note: Since  $\mathbb{Z}_4$  is an additive group, the order of an element  $a$  in  $\mathbb{Z}_4$  is the smallest positive integer  $n$  such that  $a + \cdots + a$  ( $n$  times) is equal to zero, i.e.  $na = 0$ .)

3. Reread Example 4.6. Consider the group  $U(5)$ . Is  $U(5)$  a cyclic group? If so, what elements are generators? Find the order of each element in  $U(5)$ .

4. True or False. (Give citations or counter-examples.)

(a) Every finite group is cyclic.

(b) Every cyclic group is finite.

(c) Every cyclic group is abelian.

(d) A group  $G$  is cyclic iff there is a unique element  $a$  in  $G$  such that  $G = \langle a \rangle$ .

5. What struck you in this reading? What is still unclear? What remaining questions do you have?