## Name: \_\_\_\_

Read and take notes on 18.3, Pocklington-Lehmer Criterion. Focus on Proth's Corollary, Fermat numbers, Pepin's Test, and Euler's lemma for speeding up the search for factors.

## **Reading Questions**

- 1. Make sure you are familiar with the following: Proth's Corollary, Fermat numbers, Pepin's Test, Euler's speed-up Lemma, Mersenne numbers, the Lucas-Lehmer test.
- 2. (a) In what cases is the Pocklington-Lehmer criterion especially useful?
  - (b) In what cases is it most often applied?
  - (c) How else can the technique be used, besides being used to prove primality?
- 3. Let N = 5.
  - (a) Write N in the form  $N = u2^n + 1$ , where  $u < 2^n$  and u is odd.
  - (b) Find b such that  $b^{(N-1)/2} = -1 \mod N$ .

(c) What does Proth's Corollary allow you to conclude about N?

4. Use Pepin's Test to show that the third Fermat number,  $F_3 = 257$ , is prime.

5. What lemma (due to Euler) allows us to speed up the search for prime factors of Fermat numbers by a factor of 128? State the lemma here.

6. Take a look at the following recent article. (The link is live in the pdf file.) What is the largest known prime number?

http://www.nytimes.com/2016/01/22/science/new-biggest-prime-number-mersenne-primes.html?\_r=0

7. What struck you in this reading? What is still unclear? What remaining questions do you have?